

NEW MODELING OF THERMAL DIVISION IN TURBULENT TUBES

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ABSTRACT: Turbulent Ranque effect is a typical macro–quantum phenomenon, which cannot be described by classical theory. About a century of unsuccessful experience in defining this phenomenon on the basis of classical methods testifies to this. The basic idea of non–local thermodynamics is to use quantum entropy, with every quantum defined as equal to Boltzman constant. This hypothesis will allow to apply thermodynamic energy. Further, correlations of quantum mechanics are used. In this article, the process of gasses’ thermal division in turbulent tubes is described on the basis of thermodynamic theory according to Newtonian time.

KEYWORDS: Non-local thermodynamic, Ranque effect, vortical tube

INTRODUCTION

Turbulent Ranque effect is a typical macro–quantum phenomenon, which cannot be described by classical theory. About a century of unsuccessful experience in defining this phenomenon on the basis of classical methods testifies to this.

Another new approach to solve this problem is using non-local version of thermodynamics, developed in the Moscow State University of Engineering Ecology [1].

The basic idea of non–local thermodynamics is to use quantum entropy, with every quantum defined as equal to Boltzman constant– k . This hypothesis will allow to apply thermodynamic energy – kT . Further, correlations of quantum mechanics are used. For brevity purposes, only the relation of energy–time is used here:

$$\Delta E \Delta t = \hbar / 2 \quad (1)$$

Using $\Delta E = kT$ in the relation (1) allows establishing the minimum interval macroscopic processes that depend only on temperature:

$$\Delta t = \frac{\hbar}{2kT} \quad (2)$$

In addition, radius r and volume V in the environment for time Δt is:

$$r = c \Delta t = \frac{c \hbar}{2kT} \quad (3)$$

$$V = (4/3) \pi r^3 = (\pi/6) (c \hbar / kT)^3 \quad (4)$$

For example, at $T = 293K$, by using relations (2), (3), (4) we will receive following results:

$$\begin{aligned} \Delta t &= 1.3 \cdot 10^{-14} \text{ s,} \\ r &= 3.9 \cdot 10^{-6} \text{ m,} \\ V &= 2.5 \cdot 10^{-16} \text{ m}^3 \end{aligned}$$

Volume V , calculated using the minimum sizes of ΔE , Δt , k on physical sense is the minimum macroscopic

volume. The enclosed area by this volume is named macro cell in non–local version of thermodynamics. The macro cell can be considered as shortly living and special physical cluster, over the molecular level in hierarchy of macroscopic system.

Characteristic of a macro cell as a physical self–reliant object is that, on the one hand, it is the maximum microscopic volume and quantum mechanics laws apply to it, and on the other hand, is the minimum macroscopic volume, to which apply minimum classical definitions. Hereafter there is a possibility of simultaneous existence of Boltzman and Planck constants at macro level.

For example, in the new approach it has been shown that the ensemble of particles in a macro cell act as a unit and their collective speed at time Δt is $v = (kT/m)^{1/2}$. In other words, in non-local version of thermodynamics, balance is considered as dynamic resilient position and for its maintenance, function of certain forces is required which depend on temperature:

$$F_m = \pm \frac{m}{\Delta t} \sqrt{\frac{kT}{m}} \quad (5)$$

It was on this basis that Ranque effect was described thermodynamically [2].

CALCULATION

For this purpose, we will start with some macroscopic elements in hydrodynamics. In the way that the macroscopic elementary stream will have the maximum section of a macro cell, the connected surface stream will have a thickness of $2r$, where r is macro cell radius. Obviously, macroscopic the elementary stream will have a radius of R with the maximum section of a macro cell.

Let the ensemble of such elementary streams have a macroscopic and connected surface stream of width b and volume $V = 2brR$, but the attached surface stream with N package will have such volume of $V_p = 2brRN$.

The mass of surface package of stream is calculated from the following relation:

$$M=2brRN\rho \tag{6}$$

where ρ indicates density, and N indicates the number of elementary surface vortex.

In a vortex tube, the centrifugal force arising in a macroscopic vortex (6) operates with angular speed ω :

$$F=M\omega^2R \tag{7}$$

Force F as an external force acts on macro cell of non-local version of thermodynamics in which operates resilient force (5).

As a result, according to the non-local version of thermodynamics, the macro cell moves from one equilibrium to another dynamic equilibrium position, observing the equality of centrifugal force and resilient inertial forces in a macro cell.

At resilient equilibrium state of this position, the other macro cell will have a new temperature according to the relation (5).

Equating (5), (7) it results in:

$$M\omega^2R = \frac{m}{\Delta t} \sqrt{\frac{kT}{m}}$$

Considering $m=V\rho$ and (6) we will have:

$$2br\omega^2R^2N\rho^{1/2} = \frac{V}{\Delta t} \sqrt{\frac{kT}{V}}$$

As $V=(4/3)\pi r^3$, $\Delta t = \hbar / 2kT$, $r = c\hbar / 2kT$, it is possible to have the following ratio:

$$b\omega^2R^2N\rho^{1/2} = aT \tag{8}$$

here $a = \pi c k (2/3\pi c\hbar)^{1/2} = 0.0337 \text{ (m.J)}^{3/2}/\text{s.K}$ (a collection of constants)

Thus, the right side of expression (8) only depends on temperature and some basic constants. Parameters in the left part depend on current vortex's radius R_i , and so we can write the following expression:

$$(\omega^2 bR^2 N\rho)_i = aT_i \tag{9}$$

Later expressions (8), (9) are the main equations for describing the regime and structural effect of parameters of Ranque vortex tube, which are obtained exclusively based on macro quantum parameters.

One can easily analyze hydrodynamic vortex attached to the tube's internal wall. For this purpose we may use linear speed in tube's entrance of vortex tube's connector, which has been calculated on the basis of entrance section of connector tube's nozzle and specific efficiency $v=2\pi R\omega$.

Whence $\omega=v/2\pi R$ and finally, from relation (7) we will get:

$$v^2bN\rho^{1/2} = a'T \tag{10}$$

here, $a'=4\pi^2a=1.3304 \text{ (m.J)}^{3/2}/\text{s.K}$, i.e. in the condition of applying optional linear speed, entrance stream of Ranque effect is determined by dependent package bN and density ρ .

Amount of selection of cold (hot) stream should be considered separately. Selection affects hydrodynamic stream. So we will consider the linear speed at tube's wall equal to $v_R=2\pi R\omega_R$ and $v_i=2\pi R_i\omega_i$. Dividing v_R on v_i we'll have:

$$v_i=v_R(R_i/R)(\omega_i/\omega_R) \tag{11}$$

The ratio of first relation decreases as the radius of vortex decreases, but the second ratio may increase which results in the decrease or increase of external stream's temperature. This naturally influences selection of hot stream.

Therefore, selection influence can lead to a minimum of external stream's temperature and a maximum of division efficiency. If we arrive at the conclusion that thermodynamic nature of all division processes is identical, optimum thermodynamic selection will have always an identical probability without any special restrictions, i.e. the ratio of selections of cold and hot streams should be equal. These facts have been proved by examinations.

RESULTS AND DISCUSSIONS

The analysis of industrial cyclone devices "NIIOGaz" type 15-Dx1YP by calculating various entrance parameters according to the obtained mathematical model (10) showed that for a regime, which its temperature has not exceeded its boiling point, just 3–12 macroscopic elementary vortexes of "solid-state" character are needed.

This analysis shows that in order to maintain required effect without exceeding boiling point, we just need to have kept a thin wall layer in dependent vortex of solid object. Such a state regarding solid object in the region of vortex tube in the Gutsol experimental work [3] has been considered based on high-speed filming.

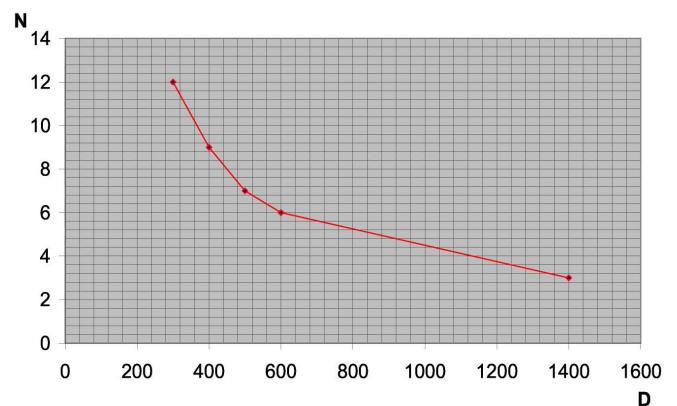


Figure 1. Changes of the number of macroscopic vortexes as compared to diameter of vortex tube for the (calculation) devices.

To analyze the mentioned method, experimental data of PhD thesis of doctorate student of Moscow State University of Engineering, M.A. Terekhov, which was done under supervision of Professor O.A. Troshkin [4], were used.

Researches were done on a Ranque tube with separable box's diameter of $D=18\text{mm}$; and length of $L=125\text{mm}$. The experimental stand was equipped by the modern measurement and control set of equipments and automation equipments and advanced integral software programs.

Of experimental data, all regime parameters, which are used in the formula (10), except the number of macroscopic elementary dependent vortex, are clear in the package N. Their number was calculated 16 with general thickness of $2rN=0.11\text{mm}$.

For comparison it should be noted that in this experiment there are $h/2r=513$ dependent elementary macroscopic layer in the opening of entrance tube.

CONCLUSIONS

During processing of experimental data with various ratios of products it has been noticed that multiplication of ubN in the formula (10) changes unnoticeably by change of selection of product in the selection region of $m=0.5$.

According to this feature, thermodynamic method of the analysis of the vortex equipments was formulated, and following results were obtained accordingly:

1- On the basis of regime and structural parameters of vortex tube, the number of elementary macroscopic vortex for the regime of vortex tube N without exceeding of temperature from boiling point was calculated:

$$N=4\pi^2 aT\rho^{3/4} bh^2 \mathcal{G}^2$$

2- The analysis of the received result was carried out. There should be enough macroscopic vortexes so that the increase of vortex's width (b) when the stream enters the vortex tube, does not lead to decrease of wave to $N<1$. On the opposite, macroscopic vortex will transform to a microscopic state, which is the state of non-formation of stream's cooling effect. To avoid this state, we may increase N against what we did at first and change the regime and structural parameters of device.

3- Recommended radius of selection of hot stream with theoretical justification in $m=0.5$:

$$R_k=R-(1/2) h$$

4- We can estimate ideal of stream for macroscopic state by using information entropy of Shannon for two streams at the state of $m=0.5$:

$$\begin{aligned} \frac{T_{in} - T_c}{T_{in}} &= \frac{\Delta T_c}{T_{in}} = H = \\ &= -m \ln m - (1-m) \ln(1-m) = \\ &= \ln 2 = 0.693. \end{aligned}$$

5- Real efficiency of cooling could be estimated. For an analyzed vortex tube this size equals to $(\frac{\Delta T_c}{T_{in}}) = 0.0741$. Hence, the coefficient of thermodynamic positive function will read: $0.0741/0.693 = 0.107$.

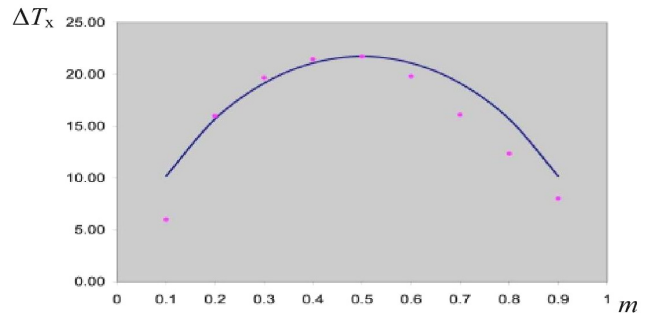


Fig.2. Comparison of the computational data with experimental data
Calculation —, Experiment •••••
($T=293\text{K}$, $G=0,0032\text{kg/s}$, $P=168\text{KPa}$)

As you see, the approach of thermodynamic calculation can be applied for other separator (dividing) systems [5].

Symbols. Subscripts

- c – Velocity of light in vacuum, $c = 2.998108\text{m/s}$
- F_m - Inertial force in a macro cell, N
- \hbar – Planck's constant, $\hbar = 1.055 \cdot 10^{-34} \text{J.s}$
- k – Boltzma's n constant, $k = 1.381 \cdot 10^{-23} \text{J/K}$
- m – Weight of a macro cell, kg
- M – Molecular weight, kg/kmol
- P – Pressure, N/m^2
- R_i – Radius of a current whirlwind, m
- r – Macro cell radius, m
- T – Absolute temperature, K
- Δt - The minimum macroscopical time scale, s
- ρ – Density, kg/m^3
- ω – Frequency (angular speed), 1/s
- D (R) – Diameter (radius) of a vortex tube, m
- L – Length, m
- m – Relative (dimensionless) share of cold stream
- Q – The volume expense, m^3/s
- u – Linear speed, m/s
- V – Whirlwind volume, m^3
- c – Cooled stream

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