



<sup>1.</sup> Stevan MAKSIMOVIĆ, <sup>2.</sup> Mirjana **Đ**URIĆ, <sup>3.</sup> Mirko MAKSIMOVIĆ, <sup>4.</sup> Ivana VASOVIĆ

# FATIGUE LIFE ESTIMATION OF AIRCRAFT STRUCTURAL COMPONENTS WITH SURFACE CRACKS UNDER LOAD SPECTRUM

<sup>1,2</sup> Military Technical Institute, Belgrade, SERBIA <sup>3.</sup> Waterworks and Sewerage, Belgrade, SERBIA <sup>4</sup> Institute GOSA, MilanaRakica 35, Belgrade, SERBIA

Abstract: Subject of this work is focused to developing computation procedure for residual fatigue life estimation of cracked structural componentsunder load spectrum. Finite element method is used for determination of the stress intensity factors (SIF's) of structural element with surface cracks. These discrete values of the stress intensity factors of cracked structural componentsare used for derivation of analytic function for SIF that is necessary in crack growth analyses. To demonstrate efficient computation procedure in residual fatigue life estimation of damaged structural elements here numerical examples are included. For residual life estimation of cracked structural elements here Forman and Mettumethod is used. In this approach a low cyclic fatigue material properties are used. Computation procedure to strength analyze with respects to fracture mechanic and residual life estimations is applied to aircraft structural elements with surface cracks under load spectrum. Computation results are compared with correspond analytic experimental results.

Keywords: Fatigue, stress intensity factors, surface cracks, singular finite elements, fatigue life prediction

### INTRODUCTION

Throughout their service life, aircraft are subjected method. The slice synthesis method has also proved to the combination of environmental attack and to be an accurate an inexpensive method to varying loads. The structural integrity of the vehicle compute 3D stress intensity factor solutions [4-6]. can be impaired by surface degradation due to The most accepted stress intensity factor solutions corrosive action or when crack damage is developed for surface cracks in finite thickness plates are or aggravated by the environment. The requirement obtained using FEM [3,4]; other methods are for lightweight aerospace structures leads to high usually compared with FEM solutions to confirm design stresses [1]. High stresses can produce cracks their accuracy and convergence. early in the fatigue life of these structural The methodology used here involves use the slice components.Surface and corner cracks encountered in engineering structures at locations technique. where high stresses. Such cracks are present during STRESS INTENSITY FACTORS OF SEMI-ELIPTIC a large percentage of the useful life of these SURFACE CRACK components. Accurate stress intensity factors for The slice synthesis approach used herein to such cracks are necessary for reliable prediction of computation of surface flaw stress intensities. The fatigue crack growth rates or fracture. Three- three dimensional surface flaw is idealized as a system dimensional (3-D) stress configurations have received considerable attention crack whose length is determined by locations thru in the literature in the last three decades [2-4]. the thickness at which the slice was taken, Figure 2. Various methods have been used to obtain stress- Each slice is considered to react independently to the intensity factors for surface and corner cracks in applied stress,  $\sigma$ , but are coupled through the plates: the alternating method [1,2], the finite- introduction of pressure distribution, p\*, acting on the element method (FEM) with singularity elements faces of the cracks. The pressure p\*, is determined by

hybrid elements and finite element alternating

are synthesis method that utilizes weight function

analysis of crack of slices in the x-y plane, each containing a center [6], the finite element method with displacement second system of slices in the z-y plane. Each of the z-





# ACTA TEHNICA CORVINIENSIS Bulletin of Engineering

#### Fascicule 2 [April – June] Tome IX [2016]

# y slices contains an edge crack of depth a(x) over NUMERICAL EXAMPLES

which the pressure, p\*, acts in opposition to that Finite element analysis for surface cracks Figure 2.







The weight function in this case was formulated in the same manner as that of Fujimoto[5]. Using the crack face pressure distributions, stress intensity factors at A and B can be determined as

$$K_{A} = \sigma \sqrt{\pi a} \sum_{i=0}^{3} \sum_{j=0}^{3} A_{ij} \left(\frac{c}{a}\right)^{i/2} \left(\frac{a}{t}\right)^{i} \qquad (1)$$

$$K_{B} = \sigma \sqrt{\pi a} \sum_{i=0}^{3} \sum_{j=0}^{3} B_{ij} \left(\frac{\mathbf{c}}{a}\right)^{i/2} \left(\frac{\mathbf{a}}{t}\right)^{i}$$
(2)

where: K<sub>A</sub> is the stress intensity at depth; K<sub>B</sub> is the stress intensity at surface,  $\sigma$  -applied stress, a - crack depth, c ~ half surface length, t ~ plate thicknes;  $A_{ii}$ are the coefficients (represent the and  $B_{ii}$ displacements over the entire crack face, the continuity expression is evaluated at 13 points).

To validate the analytic computation procedure, finite element method is used. Three-dimensional finite elements were used to model a plate Results presented in Figure 3 give good agreement containing a semi-elliptic surface crack. The finite between presented computation analytic and finite element analyses were made using MSC/NASTRAN element results for the stress intensity factors. The [8].

applied to the center crack slices [5]. Thus there are To check validity of the above method for SIF two slice systems: center cracks, and edge cracks, evaluation by the semi-analytic slice synthesis approach, comparison between the calculated SIF results of surface cracks in plate and the solution obtained by finite elements are compared. For this purpose plate with semi-elliptic surface crack under tension  $\sigma = 83.3$  [N/mm<sup>2</sup>] is analyzed. Geometry properties of this plate are: w=60 mm, t=10 mm, c=10 mm, a=10 mm, Figure 2. Threedimensional singular finite elements were used to model of a plate containing a semi-elliptic surface cracks under tensile load.



Figure 2. Detail finite element model of semi-elliptic crack



Figure 3. Comparisons between analytic and FE results for SIF calculations

difference was found to be less than 6%.

### Fatigue crack growth

The stress-intensity factor equations (1) and (2) for surface cracks are used herein to predict fatiguecrack-growth patterns under load spectra, Figure 2. confirmatequality of presented analytic method in For this purpose Forman and Mettu equation [7] is crack growth analyses. used.

$$\frac{da}{dN} = C \left[ \left( \frac{1-f}{1-R} \right) \Delta K \right]^n \frac{\left( 1 - \frac{\Delta K_{th}}{\Delta K} \right)^p}{\left( 1 - \frac{K_{max}}{K_c} \right)^q}$$
(3)

where N is the number of applied fatigue cycles, a is the crack length, R is the stress ratio,  $\Delta K$  is the stress intensity range, C, n, p and q are empirically derived constants, f is the crack opening function,  $\Delta K_{\text{th}}$  is the threshold stress intensity factor and K<sub>c</sub> is the fracture toughness.

# Numerical validation

Crack growth analysis for the next geometric and material properties of structural component with semi-elliptic surface crack, Figure 2, are illustrated in Figure 4.

- depth of surface crack, a = .100E-02 [m],half-» length of surface crack c = .100E-02 [m]
- plate thickness, t = .200E-01 [m], width of » cracked plate w = .200E-01 [m]
- crack growth coef., C = .300E 10, exponent n= » .250E+01
- fracture toughness,  $K_{IC} = .500E + 02$

Table	1.	Load	SĮ	pec	tra
-------	----	------	----	-----	-----

Ni	Smin [MPa]	Smax [MPa]
6000	0	500
6000	100	400

Figure 4 shows results of crack growth analysis under load spectra. Curves denoted as Anal-A and Anal-B represent crack growths of points A and B (Figure 2) for semi-elliptic surface cracked structural element under tension load using analytic expressions for (1) and (2) stress intensity factor calculations with one side and Forman and Mettu equation (3).

Curve denoted with MKE-B represents crack growth at point B where SIF determined using approximate finite element results. Procedure for approximations of SIF from finite elements are presented in paper [4]. This procedure is based on determination of SIF using special 3-D finite elements for several successive crack length and defining analytic expression for SIF in polynomial form from these values. This method based on using 3-D special singular quarter-point singular finite elements for determination of SIF is very reliable method. If we compare crack growth in point B using analytic REFERENCES approach derived in previous considerations with [1] Broek, D.: (1989), The Practical uses of fracture finite element results (FEM-B) good agreement is between evident.Good agreement computation method based on slice synthesis method with finite element approximations of SIF





# 4. CONCLUSION

Stress intensity factor solutions for semi-elliptical surface cracks were determined using analytic model and validation by comparisons with special singular finite element solutions. The slice synthesis approach is used herein to computation of surface flaw stress intensities. To validate the analytic derived stress intensity factors for semi-elliptic surface cracks, finite element method is used. The analytic results based on slice synthesis method were compared with finite element solutions and the difference was found to be less than 6% for surface points. Analytic model for the stress intensity factors, derived in this work, are used for crack growth analyses and fatigue life predictions.

#### Acknowledgments:

The authors would like to thank the Ministry of Education and Science of Serbia for financial support under the project number OI 174001 and TR 34028.

# Note

This paper is based on the paper presented at The 12th International Conference on Accomplishments in Electrical and Mechanical Engineering and Information Technology - DEMI 2015, organized by the University of Banja Luka, Faculty of Mechanical Engineering and Faculty of Electrical Engineering, in Banja Luka, BOSNIA & HERZEGOVINA (29th - 30th of May, 2015), referred here as [9].

- mechanics, Kluwer Academic Publishers.
- analytic [2] Maksimović, S., Vasović, I., Maksimović, M., Đurić, M.(2011). Residual life estimation of damaged structural componentsusing low-cycle

fatigue properties. Third Serbian (28th Yu) Congress on Theoretical and Applied Mechanics, Vlasina lake, Serbia, 5-8 July 2011; Serbian Society of Mechanics, Belgrade; COBISS: SR-ID 187662860; 2011; pp.605 – 617.

- Blažić, M., Maksimović, K., Assoul,Y. (2011) Determination of stress intensity factors of structural elements by surface cracks, Third Serbian Congress Theoretical and Applied Mechanics, Vlasina Lake, 5-8 July 2011, pp. 374-383, Organized: Serbian Society of Mechanics, COBISS:SR-ID 187662860, 531/534(082).
- [4] Maksimovic, S., Maksimovic, K. (2012), Improved computation method in residual life estimation of structural components, Theoretical and Applied Mechanics, Special Issue – Adress to Mechanics, Vol. 40 (S1), 2012, pp. 223-246, doi: 10.2298/TAM12S1247M. (ISSN 1450-5584).
- [5] Fujimoto,W.T. (1976), Determination of crack growth and fracture toughness parameters for surface flaws emanating from fastener holes, MDC Report A4093, 17 March 1976, Presented at the AIAA; ASME/SAE 17th SDM Meeting, Valley Forge, Pa., 4-7 May 1976.
- [6] Barsoum, R.S. (1977), Triangular quarter-point elements as elastic and perfectly-plastic crack tip elements, Int. J. Numer. Meth. Engng., 11, pp. 85-98.
- [7] Forman, R.G., Mettu, S.R. (1992), Behavior of surface and corner cracks subjected to tensile and bending loads in Ti-6Al-4V Alloy, Fracture Mechanics: Twenty-second Symposium, Vol.1, ASTM STP 1131, H.A.Ernst, A.Saxena, and D.L.McDowell, eds., American Society for Testing and Materials, Philadelphia,pp.519-546.
- [8] Msc/NASTRAN software code ~ Theoretical Manuals.
- [9] Maksimović, S., Đurić, M., Maksimović, M., Vasović, I., Fatigue life estimation of aircraft structural components with surface cracks under load spectrum, The 12th International Conference on Accomplishments in Electrical and Mechanical Engineering and Information Technology – DEMI 2015







http://acta.fih.upt.ro